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# A fast maximum likelihood nonlinear feature transformation method for GMM-HMM speaker adaptation

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#### ABSTRACT

We describe a novel maximum likelihood nonlinear feature bias compensation method for Gaussian mixture\_model\_hidden Markov model (GMM-HMM) adaptation. Our approach exploits a single-hidden-layer neural network (SHLNN) that, similar to the extreme learning machine (ELM), uses randomly generated lower-layer weights and linear output units. Different from the conventional ELM, however, our approach optimizes the SHLNN parameters by maximizing the likelihood of observing the features given the speaker-independent\_GMM-HMM. We derive a novel and efficient learning algorithm for optimizing this criterion. We show, on a large vocabulary speech recognition task, that the proposed approach can cut the word error rate (WER) by 13% over the feature maximum likelihood linear regression (fMLLR) method with bias compensation, and can cut the WER by more than 5% over the fMLLR method with both bias and rotation transformations if applied on top of the fMLLR. Overall, it can reduce the WER by more than 27% over the speaker-independent system with 0.2 real-time adaptation time.

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#### 1. Introduction

Automatic speech recognition (ASR) systems rely on powerful statistical techniques such as Gaussian mixture model—hidden Markov models (GMM–HMMs) [1] and deep neural network (DNN)-HMMs [2] to achieve good performance. Even though ASR systems are trained on large amounts of data, mismatches between the training and testing conditions are still unavoidable due to speaker and environment differences. Much like other systems built upon statistical techniques, ASR systems often fail to produce the same level of performance when tested under mismatched conditions.

A substantial amount of work has been conducted to improve ASR systems' performance under mismatched conditions. A comprehensive review of existing techniques can be found in [3]. The key idea of these techniques is to adapt either the model or the feature so that the mismatch between the training and testing conditions can be reduced. Here we briefly review the three techniques that motivated this work.

The first class of techniques adapts the model or feature by applying the physical model that causes the mismatch [4–6]. For example, the parallel model combination (PMC) method [4] adapts the speech models under noisy environment by combining

clean speech models and noise models. The joint additive and convolutive noise compensation (JAC) [5] method jointly compensates for the additive background noise and channel distortion by applying the vector Taylor series expansion of the physical distortion model around the mean vectors of clean speech, noise and channel. Methods in this category differ on the type of physical models used and the approximation applied. For instance, the JAC method may be further improved by including both the magnitude and phase terms in the physical model that describes the relationship between speech and noise [6].

The second class of techniques [7,8] adapts the model or feature by learning the distortion model from stereo data, i.e., data recorded simultaneously over a "clean" and "noisy" channel. Methods in this category differ in how the distortion model is estimated and used to compensate for the mismatches during testing.

In contrast to the above techniques, the third class of technique does not need an explicit model that describes how speech is distorted. Instead it learns a transformation directly from the adaptation data and the associated transcriptions that may contain errors. This transformation is then used either to modify the test features to make it closer to the training data or to adjust the HMM model so that it better represents the test data. Example methods in this category include stochastic matching [9] and the popular maximum likelihood linear regression (MLLR) [10]. This class of techniques is more flexible than the first class of techniques since it does not rely on a physical model, which may not be available when, for instance, the HMMs are trained on noisy

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speech. This class of techniques is also less demanding than the second class of techniques since it does not require stereo data which are rarely available. For these reasons this class of techniques has been widely used in real world large vocabulary speech recognition (LVSR) systems while the first and second class of techniques are mainly successful in small tasks such as digits recognition in noisy conditions [11,12]. Due to the large amount of HMM parameters involved in LVSR systems, feature transformation is preferred over model adaptation [10] to reduce computational cost.

Effort has been made to extend the third class of techniques to deal with nonlinear distortions. For example, in [13] a single-hidden-layer neural network (SHLNN) was used to estimate the nonlinear transformations to adapt the HMM model or feature. A gradient ascent method was developed to estimate both the upper- and lower-layer weights of the neural network, which unfortunately, was slow to convergence and easy to overfit to the training data [13] especially since the adaptation dataset is typically very small. Furthermore, the neural network in [13] was trained to maximize the likelihood of the transformed feature instead of the observed feature, which requires considering the Jacobian of the feature transformation.

Recently, extreme learning machine (ELM) [14] was proposed to address the difficulty and inefficiency in training single-hidden-layer neural networks. There are two core components in the ELM: using randomly generated "fixed" connection between the input and hidden layer (called lower-layer weights) and using linear output units so that for minimum mean square error criterion closed-form solution is available when the lower-layer weights are fixed. The randomly generated lower-layer weights are independent of the training data and so ELM is less likely to overfit to the training data than the conventional neural networks. ELM has been used as building blocks for example in the deep convex network (DCN) [15,16].

In this paper we propose a novel nonlinear feature adaptation framework for LVSR exploiting the core ideas in ELM. More specifically, we estimate a nonlinear time-dependent bias using an ELM-like SHLNN to compensate for the mismatch between the training and testing data. In this SHLNN, the lower-layer weights are randomly generated and the output layer contains only linear units just as in the ELM. Different from ELM, however, the SHLNN in our task is optimized to maximize the likelihood of either the transformed feature, for which a closed-form solution is derived, or the observed feature, for which an efficient second-order Gauss-Newton method is developed.

Our approach belongs to the third class of adaptation technique just reviewed. It requires neither physical models nor stereo data and can be easily applied to LVSR tasks. Our proposed approach is also more powerful than the previously developed approaches because it can take advantage of the neighboring frames (e.g., [4,6,5,10,13] cannot) and uses nonlinear transformations (e.g., [17] does not). We show, on a large vocabulary speech recognition task, that the proposed approach can cut the word error rate (WER) by 13% over the feature maximum likelihood linear regression (fMLLR) method with bias compensation, and can cut the WER by more than 5% over the fMLLR method with both bias and rotation transformations if applied on top of the fMLLR. Overall, it can reduce the WER by more than 27% over the speaker-independent system.

The rest of the paper is organized as follows: in Section 2, we discuss the problem of feature space transformation for speaker adaptation. In Section 3 we present the training algorithms of the ELM-like SHLNN for maximizing the likelihood of the transformed feature and observed feature and describe a tandem scheme that applies the nonlinear transformation on top of the linearly transformed feature. Experimental results are reported in Section 4 to

demonstrate how hidden layer size and context window lengths affect the adaptation effectiveness and how the proposed approach outperforms fMLLR on an LVSR task. We conclude the paper in Section 5.

## 2. Speaker adaptation through nonlinear feature transformation

In contrast to the traditional feature space transformation [9,10,17] that is a linear transform of observation vector  $\mathbf{x}_t$  at time t, the method presented in this paper is a nonlinear feature transformation method.

The nonlinear feature transformation can be defined as  $f(\overline{\mathbf{x}}_t, \boldsymbol{\phi}_t)$ , where  $\boldsymbol{\phi}_t$  is a meta feature vector that contains information such as signal-to-noise ratio and utterance length,  $\overline{\mathbf{x}}_t \in R^{LD}$  is an expanded observation vector centered at  $\mathbf{x}_t \in R^D$  with a context length of L. For example, for a context length of L=3,  $\overline{\mathbf{x}}_t = (\mathbf{x}_{t-1}^T \mathbf{x}_t^T \mathbf{x}_{t+1}^T)^T$ , where superscript T denotes transpose. Usually,  $\overline{\mathbf{x}}_t$  is augmented with element 1 to become  $(\overline{\mathbf{x}}_t^T 1)^T$ .

For speech recognition, the transformation  $f(\overline{\mathbf{x}}_t, \boldsymbol{\phi}_t)$  is typically optimized to improve the likelihood of the observed feature  $p(\mathbf{x}_t|\Theta,\Lambda_x)$ . Here  $\Theta$  denotes parameters of the nonlinear transformation and  $\Lambda_x$  denotes speaker independent HMM parameters that include (GMM) parameters  $\{\pi_m, \boldsymbol{\mu}_m, \boldsymbol{\Sigma}_m; m=1,...,M\}$  and state transition probabilities  $\{c_{ij}; i,j=1,...,S\}$ , where M is the total number of Gaussian components, S is the number of states, and  $\pi_m$ ,  $\boldsymbol{\mu}_m$  and  $\boldsymbol{\Sigma}_m$  are the weight, mean vector and diagonal covariance matrix, respectively, of the m-th Gaussian component.

Directly improving the above likelihood is difficult. We instead iteratively estimate  $\Theta$  through the following auxiliary function:

$$\begin{aligned} &Q(\boldsymbol{\Theta}; \widetilde{\boldsymbol{\Theta}}) \\ &= -\frac{1}{2} \sum_{m,t} \gamma_m(t) (f(\overline{\mathbf{x}}_t, \boldsymbol{\phi}_t) - \boldsymbol{\mu}_m)^T \boldsymbol{\Sigma}_m^{-1} (f(\overline{\mathbf{x}}_t, \boldsymbol{\phi}_t) - \boldsymbol{\mu}_m) \\ &+ \sum_{m,t} \gamma_m(t) \log |\mathbf{J}_t| \end{aligned} \tag{1}$$

where  $\widetilde{\Theta}$  is the previous estimate of  $\Theta$ ,  $\gamma_m(t)$  is the posterior probability of Gaussian m at time t, given HMM parameters  $\Lambda_x$  and the previous estimates of the nonlinear transformation parameters  $\widetilde{\Theta}$ .  $\mathbf{J}_t = (\partial f(\overline{\mathbf{x}}_t, \boldsymbol{\phi}_t))/\partial \mathbf{x}_t$  is the Jacobian of the feature transformation at time t. Note that we assume that the feature transformation is not dependent on a particular Gaussian m.

For speaker adaptation, observation vectors  $\mathbf{x}_t$  are from a particular speaker. Increasing the above auxiliary function scores corresponds to learning a speaker dependent transformation that increases the likelihood of observation  $\mathbf{x}_t$ , given the GMM parameters.

Theoretically the transformation function  $f(\overline{\mathbf{x}}_t, \boldsymbol{\phi}_t)$  can be any function. In this paper we focus on compensating for the bias change, i.e.,

$$\mathbf{y}_{t} = f(\overline{\mathbf{x}}_{t}, \boldsymbol{\phi}_{t}) = \mathbf{x}_{t} + g(\overline{\mathbf{x}}_{t}, \boldsymbol{\phi}_{t}), \tag{2}$$

where  $g(\overline{\mathbf{x}}_t, \pmb{\phi}_t)$  is a nonlinear function compensating for the bias and is defined by the SHLNN shown in Fig. 1. Similar to the ELM, the SHLNN consists of a linear input layer, a sigmoid nonlinear hidden layer, and a linear output layer. The SHLNN parameters  $\Theta$  include a  $D \times K$  matrix  $\mathbf{U}$ , a  $K \times LD$  matrix  $\mathbf{W}$  and a scalar value  $\alpha$ , where  $\mathbf{U}$  is the upper layer weights connecting the hidden layer and the output layer,  $\mathbf{W}$  is the lower layer weights connecting the input layer and the hidden layer, and  $\alpha$  is the parameter to control steepness of the sigmoid function at the hidden layer. Since  $\pmb{\phi}_t$  can be considered as part of the observation we merge  $\pmb{\phi}_t$  into  $\overline{\mathbf{x}}_t$  from now on to simplify notation.

**Eq.** (2) can be further rewritten and simplified to

 $\mathbf{y}_t = \mathbf{x}_t + \mathbf{U}\mathbf{h}_t \tag{3}$ 

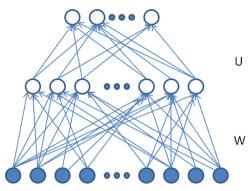


Fig. 1. Neural network architecture.

where  $\mathbf{h}_t = \boldsymbol{\theta}(\alpha \mathbf{W} \, \overline{\mathbf{x}}_t)$  is the hidden layer output and  $\boldsymbol{\theta}(x) = 1/(1 + \exp(-x)) = \exp(x)/(1 + \exp(x))$  is the sigmoid function, by noting that, following ELM, the lower-layer weight  $\mathbf{W}$  is randomly generated and is independent of the adaptation data and the training criterion. The scalar value  $\alpha$  is typically set to a value around 1.0. In this paper, it is set to 0.6.

#### 3. The algorithms for maximum likelihood estimation

As we discussed in the last section, the only parameter set we need to learn is **U**, whose algorithm will be derived in this section. Substituting (3) into (1), we have

$$Q(\boldsymbol{\Theta}; \boldsymbol{\Theta})$$

$$= -\frac{1}{2} \sum_{mt} \gamma_m(t) (\mathbf{U} \mathbf{h}_t - \boldsymbol{\rho}_{mt})^T \boldsymbol{\Sigma}_m^{-1} (\mathbf{U} \mathbf{h}_t - \boldsymbol{\rho}_{mt})$$

$$+ \sum_{t} \gamma_m(t) \log |\mathbf{J}_t|, \tag{4}$$

where  $\rho_{mt} = \mu_m - \mathbf{x}_t$ . The Jacobian  $\mathbf{J}_t = (\partial \mathbf{y}_t / \partial \mathbf{x}_t) \in \mathbb{R}^{D \times D}$  is

$$\mathbf{J}_{t} = \mathbf{I}_{D \times D} + \alpha \mathbf{U} \mathbf{H}_{t} (\mathbf{I}_{K \times K} - \mathbf{H}_{t}) \mathbf{W}_{c}$$
 (5)

where  $\mathbf{W}_c \in R^{K \times D}$  is a submatrix of  $\mathbf{W}$ , whose rows correspond to the center observation  $\mathbf{x}_t$  in the context window,  $\mathbf{H}_t \in R^{K \times K}$  is a diagonal matrix with element  $\boldsymbol{\theta}(\alpha \mathbf{W} \, \overline{\mathbf{x}}_t)$ , and  $\mathbf{I}_{l \times l} \in R^{l \times l}$  is an identity matrix.

 ${\bf U}$  can be learned with the gradient ascent algorithm, which iteratively updates an estimate of  ${\bf U}$  as

$$\mathbf{U} \leftarrow \mathbf{U} + \eta \frac{\partial Q}{\partial \mathbf{U}},\tag{6}$$

where  $\eta$  is the step size,

$$\frac{\partial Q}{\partial \mathbf{U}} = -\sum_{m,t} \gamma_m(t) \mathbf{\Sigma}_m^{-1} (\mathbf{U} \mathbf{h}_t - \boldsymbol{\rho}_{mt}) \mathbf{h}_t^T + \sum_{m,t} \gamma_m(t) \frac{\partial \log |\mathbf{J}_t|}{\partial \mathbf{U}}$$
(7)

and

$$vec\left(\frac{\partial \log |\mathbf{J}_t|}{\partial \mathbf{U}}\right)^T = vec(\mathbf{J}_t^{-T})^T \frac{\partial \mathbf{J}_t}{\partial \mathbf{U}}$$
$$= vec(\mathbf{J}_t^{-T})^T [\alpha(\mathbf{H}_t(\mathbf{I}_{K \times K} - \mathbf{H}_t)\mathbf{W}_c)^T \otimes \mathbf{I}_{D \times D}]$$
(8)

where  $vec(\cdot)$  is a vectorization operation to stack columns of a matrix. To obtain  $(\partial \log |\mathbf{J}_t|/\partial \mathbf{U}) \in R^{D \times K}$ , we need to reshape the above vector to a  $D \times K$  matrix.

#### 3.1. Maximum likelihood estimation on transformed features

We rewrite the auxiliary function as

$$Q(\mathbf{U}, \widetilde{\mathbf{U}}) = -\frac{1}{2} \sum_{m,t} \gamma_m(t) (\mathbf{U} \mathbf{h}_t - \boldsymbol{\rho}_{mt})^T \boldsymbol{\Sigma}_m^{-1} (\mathbf{U} \mathbf{h}_t - \boldsymbol{\rho}_{mt})$$
(9)

by ignoring the Jacobian, where  $\widetilde{\mathbf{U}}$  is the previous estimate of the upper layer weights  $\mathbf{U}$ . This simplified auxiliary function maximizes the likelihood of the transformed data  $p(\mathbf{y}_t|\mathbf{U},\Lambda_x)$ , rather than the observed data  $p(\mathbf{x}_t|\mathbf{U},\Lambda_x)$ .

A closed-form solution can be obtained for the above optimization problem by running one iteration of Gauss-Newton update and setting the initial  $\mathbf{U} = 0$ . This is because the criterion (9) is a quadratic function of  $\mathbf{U}$  and its gradient is linear. Using the Gauss-Newton method, we have

$$vec(\mathbf{U}) = -\left(\frac{\partial^{2} Q}{\partial \mathbf{U}^{2}}\right)^{-1} vec\left(\frac{\partial Q}{\partial \mathbf{U}}\right)\Big|_{\mathbf{U} = 0}$$

$$= -\left(\frac{\partial^{2} Q}{\partial \mathbf{U}^{2}}\right)^{-1} vec\left(\sum_{mt} \gamma_{m}(t) \mathbf{\Sigma}_{m}^{-1} \boldsymbol{\rho}_{mt} \mathbf{h}_{t}^{T}\right)\Big|_{\mathbf{U} = 0}$$
(10)

where

$$\frac{\partial^2 Q}{\partial \mathbf{U}^2}\Big|_{U=0} = -\sum_{mt} \gamma_m(t) (\mathbf{h}_t \mathbf{h}_t^T \otimes \mathbf{\Sigma}_m^{-1})$$
(11)

using matrix calculus [18] and  $\otimes$  is the Kronecker product.

The term (11) can be written in detail as

$$\sum_{mt} \gamma_m(t) (\mathbf{h}_t \mathbf{h}_t^T \otimes \mathbf{\Sigma}_m^{-1})$$

$$= \sum_{mt} \gamma_m(t) \begin{pmatrix} h_{t1} h_{t1} \frac{1}{\sigma_{m1}^2} & \cdots & 0 & \cdots & h_{t1} h_{tK} \frac{1}{\sigma_{m1}^2} & \cdots & 0 \\ \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ 0 & \cdots & h_{t1} h_{t1} \frac{1}{\sigma_{mD}^2} & \cdots & 0 & \cdots & h_{t1} h_{tK} \frac{1}{\sigma_{mD}^2} \\ h_{t2} h_{t1} \frac{1}{\sigma_{m1}^2} & \cdots & 0 & \cdots & h_{t2} h_{tK} \frac{1}{\sigma_{m1}^2} & \cdots & 0 \\ \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ 0 & \cdots & h_{t2} h_{t1} \frac{1}{\sigma_{mD}^2} & \cdots & 0 & \cdots & h_{t2} h_{tK} \frac{1}{\sigma_{mD}^2} \\ \vdots & \cdots & \vdots & \cdots & \vdots & \cdots & \vdots \\ h_{tK} h_{t1} \frac{1}{\sigma_{m1}^2} & \cdots & 0 & \cdots & h_{tK} h_{tK} \frac{1}{\sigma_{m1}^2} & \cdots & 0 \\ \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ 0 & \cdots & h_{tK} h_{t1} \frac{1}{\sigma_{mD}^2} & \cdots & 0 & \cdots & h_{tK} h_{tK} \frac{1}{\sigma_{mD}^2} \end{pmatrix}$$

where  $h_{ti}$  denotes the *i*-th element in the hidden layer output  $\mathbf{h}_{t}$ . The memory for evaluating this term is  $O(DK \times DK)$ . For a setup with D=39 and K=2000, the cost is  $6.09 \times 10^9$  floating points, which corresponds to 48 G byte of memory. A typical computer cannot hold such large memory.

Notice that the above terms (11) and (14) are full but sparse matrices because  $\Sigma_m$  is diagonal. Fortunately a memory and CPU efficient algorithm can be derived by using the permutation matrix [18]. The intuition behind the algorithm is re-arranging the above full but sparse matrices in (14) to be block-diagonal. A permutation matrix  $\mathbf{T}_{m,n} \in R^{mn \times mn}$  is a matrix operator composed of 0s and 1s, with a single 1 on each row and column. It has a number of special properties. Particularly,  $\mathbf{T}_{m,n}^{-1} = \mathbf{T}_{n,m} = \mathbf{T}_{m,n}^T$  and  $\mathbf{T}_{m,n} vec(A) = vec(A^T)$ .

Note that

$$\mathbf{h}_{t}\mathbf{h}_{t}^{T}\otimes\mathbf{\Sigma}_{m}^{-1}=\mathbf{T}_{K,D}\mathbf{\Sigma}_{m}^{-1}\otimes\mathbf{h}_{t}\mathbf{h}_{t}^{T}\mathbf{T}_{D,K}.\tag{13}$$

Substituting this to (11), we have

$$\frac{\partial^2 Q}{\partial \mathbf{U}^2}\Big|_{U=0} = -\mathbf{T}_{K,D} \left( \sum_{mt} \gamma_m(t) \mathbf{\Sigma}_m^{-1} \otimes \mathbf{h}_t \mathbf{h}_t^T \right) \mathbf{T}_{D,K}$$
(14)

 $<sup>^1</sup>$  The scalar value  $\alpha$  was experimented with 0.6 and 1.0. We did not observe much performance differences. Hence, this paper only reports results in Section 4 with  $\alpha\!=\!0.6$ .

By applying (14) to (10) we get

$$vec(\mathbf{U}) = \mathbf{T}_{K,D} \left( \sum_{mt} \gamma_m(t) \mathbf{\Sigma}_m^{-1} \otimes \mathbf{h}_t \mathbf{h}_t^T \right)^{-1} \mathbf{T}_{D,K} vec \left( \frac{\partial Q}{\partial \mathbf{U}} \right) |_{\mathbf{U} = 0}$$

After some manipulations detailed in Appendix A.1, we get the closed-form solution at d-th row of  $\mathbf{U}$ ,  $\mathbf{U}_{d,:}$ , for  $d = \{1, \dots, D\}$  as

$$vec(\mathbf{U}_{d,:}) = \left(\sum_{mt} \gamma_m(t) \frac{1}{\sigma_{md}^2} \mathbf{h}_t \mathbf{h}_t^T\right)^{-1} vec\left(\frac{\partial Q}{\partial \mathbf{U}_{d,:}}\right) \Big|_{U=0}, \ d = \{1, ..., D\}$$
(1)

where  $\sigma_{md}^2$  is the (d,d)-th element of the diagonal covariance matrix  $\varSigma_m$ 

This corresponds to re-arranging the term (14) into the following block diagonal matrix:

$$\sum_{mt} \gamma_m(t) \begin{pmatrix} h_{t1} h_{t1} \frac{1}{\sigma_{m1}^2} & \cdots & h_{t1} h_{tK} \frac{1}{\sigma_{m1}^2} & \cdots & 0 & \cdots & 0 \\ \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ h_{tK} h_{t1} \frac{1}{\sigma_{m1}^2} & \cdots & h_{tK} h_{tK} \frac{1}{\sigma_{m1}^2} & \cdots & 0 & \cdots & 0 \\ 0 & \cdots & 0 & \ddots & 0 & \cdots & 0 \\ \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & \cdots & h_{t1} h_{t1} \frac{1}{\sigma_{m0}^2} & \cdots & h_{t1} h_{tK} \frac{1}{\sigma_{m0}^2} \\ \vdots & \ddots & \vdots & \cdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & \cdots & h_{tK} h_{t1} \frac{1}{\sigma_{m0}^2} & \cdots & h_{tK} h_{tK} \frac{1}{\sigma_{m0}^2} \end{pmatrix}$$

Keeping only the nonzero block diagonal matrices, now the total memory cost is  $O(D \times K \times K)$ . In terms of the computational cost, the matrix inversion  $(\partial^2 Q/\partial \mathbf{U}^2)^{-1}$  in (10) is on a matrix of dimension  $KD \times KD$ . Using the new algorithm, the matrix inversion  $(\sum_{mt} \gamma_m(t)(1/\sigma_{md}^2)\mathbf{h}_t\mathbf{h}_t^T)^{-1}$  in (15) is on block diagonal matrices with dimension of  $K \times K$ . Notice that the computational cost of a typical matrix inversion algorithm such as Gauss-Jordan elimination [19] is  $O(n^3)$  for a matrix of dimension  $n \times n$ . Therefore, the new algorithm has the computational cost of  $O(D \times K^3)$  for the matrix inversion whereas the matrix inversion in (10) costs  $O(D^3 \times K^3)$  operations.

#### 3.2. Maximum likelihood estimation on observed features

To optimize for the observed features we cannot drop the Jacobian term in (4) and need to solve it using an iterative Gauss–Newton procedure

$$\mathbf{U} \leftarrow \widetilde{\mathbf{U}} - \eta \left( \frac{\partial \mathbf{Q}^2}{\partial^2 \mathbf{U}} \right)^{-1} \frac{\partial \mathbf{Q}}{\partial \mathbf{U}} \Big|_{\mathbf{U} = \widetilde{\mathbf{U}}}$$
 (17)

This procedure starts from some initial estimates, such as  $\mathbf{U} = 0$ , until a certain number of iterations is reached.

We keep the Hessian term from (11) unchanged, but include a first order differential term from (8). Applying permutation matrices as shown in Appendix A.2, we can rewrite (8) as

$$vec(\mathbf{J}_{t}^{-T})^{T}[\alpha(\mathbf{H}_{t}(\mathbf{I}_{K\times K} - \mathbf{H}_{t})\mathbf{W}_{c})^{T} \otimes \mathbf{I}_{D\times D}]$$

$$= \alpha(vec(\mathbf{J}_{t}^{-1})^{T}\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K} - \mathbf{H}_{t})\mathbf{W}_{c})^{T})^{T}$$
(18)

which is a vector of dimension  $1 \times DK$ . Its *d*-th subvector with dimension K is  $\alpha(\mathbf{J}_t^{-1})_{:d}^T(\mathbf{H}_t(\mathbf{I}_{K \times K} - \mathbf{H}_t)\mathbf{W}_c)^T$ .

Applying permutation matrices similarly as in the above section, we can write (17) as follows:

$$vec(\mathbf{U}_{d,:}) = vec(\widetilde{\mathbf{U}}_{d,:}) + \eta \left( \sum_{mt} \gamma_m(t) \frac{1}{\sigma_{md}^2} \mathbf{h}_t \mathbf{h}_t^T \right)^{-1}$$

$$\times vec\left( \frac{\partial Q}{\partial \mathbf{U}_{d,:}} \right) \Big|_{\mathbf{U} = \widetilde{\mathbf{U}}}, \ d = \{1, ..., D\}$$
(19)

To obtain  $vec(\partial Q/\partial \mathbf{U}_{d:})$ , we substitute (18) into (7); i.e.

$$vec\left(\frac{\partial \mathbf{Q}}{\partial \mathbf{U}_{d,:}}\right) = -\sum_{mt} \gamma_m(t) (\mathbf{\Sigma}_m^{-1}(\mathbf{U}\mathbf{h}_t - \boldsymbol{\rho}_{mt})\mathbf{h}_t^T)_{:,d} + \sum_{mt} \gamma_m(t) \alpha (\mathbf{J}_t^{-1})_{:,d}^T (\mathbf{H}_t(\mathbf{I}_{K \times K} - \mathbf{H}_t)\mathbf{W}_c)^T$$
(20)

Note that here we assume that Hessian  $\partial^2 Q/\partial \mathbf{U}^2$  is unchanged once it is estimated from the point  $\mathbf{U}=0$  to speed up computation. The Gauss-Newton estimate can be initialized from either  $\mathbf{U}=0$  or the closed-form solution (15). The latter provides a better initial estimate and requires fewer iterations to estimate  $\mathbf{U}$ .

#### 3.3. A tandem scheme

The proposed nonlinear bias compensation approach can be applied on top of the affine fMLLR [10]

$$\hat{\mathbf{x}}_t = \mathbf{A}\mathbf{x}_t + \mathbf{b} = \mathbf{\Psi}\boldsymbol{\xi}_t \tag{21}$$

to further improve the performance, where  $\mathbf{A} \in R^{D \times D}$  is the transformation that does rotation on the input  $\mathbf{x}_t$  at time t,  $\mathbf{b} \in R^D$  is the bias to the input, and  $\mathbf{\Psi} = [\mathbf{A}; \mathbf{b}] \in R^{D \times (D+1)}$  is the combined affine transformation.  $\boldsymbol{\xi}_t = [\mathbf{x}_t^T \mathbf{1}]^T$  is the augmented observation vector at time t. This tandem scheme can take advantage of neighboring frames and compensate for remaining nonlinear mismatches after the affine fMLLR.

#### 3.4. Computational costs

We list the computational costs to implement our algorithms in Table 1. The forward propagation process in each method estimates values such as  $\mathbf{Uh}_t$ . The backward propagation process re-estimates neural network parameters **U** and **W**. We use N to denote the number of observation frames. As described in Section 3.1, solution in (15) is not an iterative algorithm. Therefore it costs  $O(N \times L \times D \times K)$  for the forward process. The cost for solution (15) in the backward process to estimate the neural network parameters is  $O(D \times K^3)$ . Our second solution (19) using Eq. (20) needs to compute, at each time frame t, an inversion matrix  $\mathbf{J}_t^{-1}$ . Since inversion operations costs  $O(D^3)$ , which dominates the computational costs at each time frame, the cost to compute solution (19) takes  $O(N \times D^3)$ . Considering the solution (19) may take J iterations to converge, the total computational cost for (19) is therefore  $O(J \times N \times D^3)$ , which is larger than the cost for solution (15). In the forward process of solution (19), the cost to compute  $\mathbf{Uh}_t$  is  $O(J \times I)$  $N \times L \times D \times K$ ) which is higher than the forward-pass cost in solution (15) because solution (19) takes *J* iterations.

Other methods in [13] use iterative forward and backward propagation algorithms to estimate both the lower- and upperlayer weights, each costs  $O(J \times N \times L \times D \times K)$  operations to converge. According to Table 1, the cost of forward process in [13] is higher than the costs for solution (15). Moreover, since L is usually larger than D and K is approximately the same as D, the cost for backward propagation in [13] is also higher than our solutions (15) and (19). It is worth mentioning that the number of iterations J in our solutions might be smaller than that used in [13] because our solutions use Gauss-Newton method, which converges faster than

**Table 1** The computational costs to implement our algorithms. D is the feature dimension, L is the context length, K is the hidden layer size, N is the number of observation frames, and J is the number of iterations.

Method	Forward prop.	Backward prop.
Solution (15) in Section 3.1 Solution (19) in Section 3.2 Method in [13]	$O(N \times L \times D \times K)$ $O(J \times N \times L \times D \times K)$ $O(J \times N \times L \times D \times K)$	$O(D \times K^3)$ $O(J \times N \times D^3)$ $O(J \times N \times L \times D \times K)$

the gradient descent method used in [13]. Specifically, the solution (15) is a closed-form solution and converges in one iteration.

#### 3.5. Other implementation considerations

Note that we have  $\gamma_m(t)$ , the posterior probability of Gaussian m at time t, in the above algorithm. In practice, we use Viterbi alignment at the Gaussian level, so  $\gamma_m(t)$  is either 1 or 0.

For completeness, we list in Appendix A.3 auxiliary functions for fMLLR [10]. To debug our implementations, we use the scores of these auxiliary functions to compare against the scores by the proposed algorithm.

To replicate results, the randomization of  $\mathbf{W}$  starts from a fixed seed. The random values for the lower layer weights  $\mathbf{W}$  are in the range of -2.0 to 2.0.

Inputs vectors need to be normalized to be zero mean and unit variance in each input feature dimension. This improves convergence of the neural network learning.

The step size  $\eta$  is important for Gauss-Newton algorithm. The step size starts from a small value, usually  $1 \times 10^{-2}$ . If one iteration does not increase auxiliary score, the current estimate is backed to its previous estimate and the step size  $\eta$  is halved for the next iteration.

For numerical issues, the inversion of Jacobian in (8) may be implemented using singular value decomposition (SVD).

#### 4. Experiments

#### 4.1. System descriptions

We conduct automatic speech recognition (ASR) experiments on an internal Xbox voice search data set. The scenario supports distant talking voice search (of music catalog, games, movies, etc.) using a microphone array. The training set of the speakerindependent (SI) GMM-HMM system contains 40 h of Xbox voice search commands. The evaluation was conducted on data from 25 speakers. For each speaker 200 utterances are used for adaptation and 100 utterances are used for testing. The total number of test sentences is 2500 with 10,563 words. There are no overlap among training, adaptation and test sets. We use Kaldi [20] to train a weighted finite state transducer (WFST)-based recognition system [21]. The features are 13-dimension Mel filter-bank cepstral coefficients (MFCC) with delta and delta-delta coefficients. Per-device cepstral mean subtraction is applied. The SI acoustic model has 7.5 k Gaussian components trained with the standard maximum likelihood estimation (MLE) [1] procedure. We compare the proposed approaches with the baseline system without adaptation and the system using fMLLR [10].

#### 4.2. Effects of hidden layer and context window size

#### 4.2.1. Hidden layer size

We first conducted experiments to investigate how the hidden layer size K affects the performance using a development set. Notice that there are methods [22,23] to automatically decide hidden layer size. The method in [22] selects the hidden layer size by reducing its regression error to a predefined threshold. The method in [23] proposes a bound of the generalization error. The method selects the hidden layer size by maximizing the coverage of unseen samples with a constraint or by thresholding on the bound. For speech recognition task, the most direct measure of error is the word error rate. However, to our knowledge, there is not yet a method to directly relate word error rate to neural network size.

We therefore empirically investigated effects of the hidden layer size to speech recognition performance. In these experiments we used the solution (15) (i.e., optimize for the transformed features) to estimate the upper layer weights **U**. Fig. 2 summarizes the experimental results under the condition that the input dimension is set to 351 (or L=9 frames) and  $\alpha$  is set to 0.6. It can be observed that we achieved the lowest WER of 25.73% when 39 hidden units were used. Additional experiments using different input layer size indicate that the lowest WERs were typically obtained when 20–40 hidden units were used. This suggests that the optimal hidden layer size is not sensitive to the input layer size. The relatively small optimal hidden layer size is attributed to the small adaptation set used.

#### 4.2.2. Context window size

Other experiments on neural network speech recognition [2,24] suggest using 9–11 frames of context window. Notice that 9–11 frames correspond to 90–110 ms, approximately the average duration of a phone in speech signal. We therefore conducted experiments to cross validate the above recommendation using the same development set. We evaluated the impact of the context window size L to the word error rate (WER) when the hidden layer size K is fixed using the same procedure described above. Table 2 summarizes our results. From Table 2 we observe that lowest WERs can be obtained with L=9 context windows if the hidden layer size is large enough to take advantage of it.

Similar experiments were conducted using the solution (19) (i.e., optimize for the observed data), which was initialized from the closed-form solution (15) and was run for 10 iterations. In Table 3 WER results with context window size *L* set to 1, 9, and 11

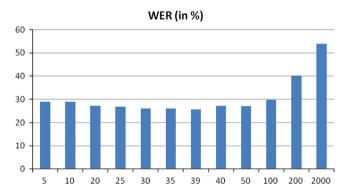


Fig. 2. The effect of hidden layer size on word error rate (WER) with solution (15). The horizontal axis is the hidden layer size.

 Table 2

 The effect of context window size on word error rate (WER) with solution (15).

Context window size	K=20	K=39
1	28.80	31.91
3	27.09	28.66
9	27.22	25.73
11	28.08	25.91

**Table 3**Effect of context window size and hidden layer size on WERs with solution (19).

Context window size	K=20	K=39
1	28.66	31.49
9	27.06	25.68
11	28.41	25.73

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and hidden layer size K set to 20 and 39 are reported. The step size  $\eta_c$  was, respectively, set to  $1\times 10^{-2}$  for context window L=1,  $5\times 10^{-3}$  for context window  $L\in\{9,11\}$  with K=20, and  $1\times 10^{-3}$  for context window  $L\in\{9,11\}$  with K=39. In all these cases, using 9-frame context provides the best WER. These experiments cross validate the recommendation of using 9-11 frames for neural network speech recognition [2,24].

**Remark 1.** It is worthwhile to point out that most previously developed methods [4,6,5,10,13] cannot take advantage of the neighboring frames, which, indicated by Tables 2 and 3, to have positive effect. [17] also benefits from the neighboring frames but uses linear model.

**Remark 2.** Notice that the closed-form solution (15) converges in one iteration and has similar performances as the iterative solution (19), which takes 10 iterations. Other existing methods [13] use the gradient descent method, therefore is even slower than the Gauss-Newton method used in the iterative solution (19). We measured the real time factor (RTF) on one speaker with the setup K=39 and L=9 that has the lowest WER. The solution (15) has RTF of 0.22 and is real time. The solution (19) has RTF of 1.21. The closed-form solution (15) therefore is desirable in conditions such as fast adaptation.

#### 4.3. Main results

Table 4 compares our proposed bias compensation approaches with the SI system and fMLLR with bias compensation [10]. In these experiments we used 9-frames of input (351 input units), 20 hidden units and 39 output units. The  $\alpha$  was set to 0.6 for the proposed approaches. The step size  $\eta$  was set to  $5 \times 10^{-3}$  and  $1 \times 10^{-3}$  for hidden layer size K set to 20 and 39, respectively.

From Table 4 we observe that fMLLR with bias compensation reduced WERs from 31.52%, achieved by the SI system, to 29.49%. This reduction is statistically significant with significance level of  $1.3 \times 10^{-3}$ . With the hidden layer size K set to 20, using our proposed approaches we can further reduce the WER to 27.22% and 27.06%, respectively, with and without dropping the Jacobian term. Compared to the fMLLR with bias compensation, our approaches cut errors by 7.7% and 8.2%. These reductions are significant, each with a significance level of  $2.5 \times 10^{-4}$  and  $8.7 \times 10^{-5}$ .

Note that the method with closed-form solution (15) without considering the Jacobian term achieved the similar performance as that with Gauss-Newton method (19). This provides a significant gain in efficiency since the closed-form solution is much faster than the Gauss-Newton method. In fact, as shown in the table, WER can be further reduced to 25.73% using the closed-form solution (15) if 39, instead of 20, hidden units are used. This translates to a relative WER reduction of 13.0% over the fMLLR with bias compensation system and is statistically significant with significance level of  $9.5 \times 10^{-10}$  [25]. The method with Jacobian term further reduced the WER to 25.68%, with the significance level of  $5.6 \times 10^{-10}$ .

**Table 4**Compare the proposed approaches with SI model and the fMLLR with bias compensation.

	WERs (%)
SI model (w/o adaptation)	31.52
fMLLR with bias compensation	29.49
Proposed approach with closed-form solution $(K=20)$	27.22
Proposed approach with Gauss-Newton method $(K=20)$	27.06
Proposed approach with closed-form solution ( $K=39$ )	25.73
Proposed approach with Gauss-Newton method ( $K=39$ )	25.68

Table 5
Compare the tandem scheme and the affine fMLLR.

	WERs (%)
Affine fMLLR Tandem scheme with closed-form solution Tandem scheme with Gauss-Newton method	24.03 22.80 22.68

The tandem scheme proposed in Section 3.3 applies both bias and rotation compensation. Table 5 compares the tandem scheme with the closed-form and the Gauss-Newton method with affine fMLLR. In these experiments a SHLNN with 9-frame input feature, 39 hidden units and 39 output units were used. The step size  $\eta$  was set to  $1\times 10^{-3}$ . As shown in this table, our proposed approaches reduced WER to 22.80% and 22.68%, respectively, with and without dropping the Jacobian term, from 24.03% achieved by affine fMLLR. These results correspond to 5.1% and 5.6% relative WER reductions with significance level of  $3.5\times 10^{-2}$  and  $2.0\times 10^{-2}$ , respectively. Compared to the SI model, our proposed methods cut WERs significantly by more than 27% with significance level of zero.

#### 5. Conclusions and discussions

In this paper, we have introduced a novel approach to train single-hidden-layer neural networks to reduce mismatch between training and testing for speaker adaptation of GMM–HMMs. The neural network may be considered as a case of the recently proposed extreme learning machine which uses randomly generated lower-layer weights and linear output units. To estimate upper layer weights, we have developed efficient closed-form solution and Gauss–Newton methods. Our proposed approach enables compensating for a time dependent bias and takes advantages of neighboring observation frames. On a large vocabulary speech recognition task, we show that the proposed approach can reduce word error rates by more than 27% over a speaker-independent system. Our proposed nonlinear adaptation approach, which uses a closed-form solution, is also significantly faster than prior arts [13] that use gradient-based methods such as back-propagation [26].

To speed up the adaptation process we have used randomly generated lower-layer weights similar to the ELM. However, trade-off may be made between the adaptation speed and the power of the model. For example, instead of using random values we may learn the lower-layer weights as well, possibly by exploiting the constraint imposed by the closed-form relationship between the weights of upper- and lower-layers. Alternatively we may stack one ELM on top of another [16,15] via input-output concatenation to increase the modeling power, which has been shown to improve phone recognition accuracy over ELM [27,28]. We believe that these extensions may further decrease the recognition error rate, at the cost of increased adaptation time.

#### Appendix A

#### A.1. Derivation of an efficient closed-form solution

Since  $\Sigma_m^{-1}$  is a diagonal matrix,  $\Sigma_m^{-1} \otimes \mathbf{h}_t \mathbf{h}_t^T$  is a block diagonal matrix. We therefore have

$$vec(\mathbf{U})$$

$$=\mathbf{T}_{K,D} \begin{pmatrix} \sum_{mt} \gamma_m(t) \sigma_{m1}^{-1} \mathbf{h}_t \mathbf{h}_t^T & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sum_{mt} \gamma_m(t) \sigma_{mD}^{-1} \mathbf{h}_t \mathbf{h}_t^T \end{pmatrix}^{-1}$$

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$$\times \mathbf{T}_{D,K} vec\left(\frac{\partial Q}{\partial \mathbf{U}}\right)|_{\mathbf{U} = 0}$$

$$= \mathbf{T}_{K,D} \begin{pmatrix} \sum_{mt} \gamma_m(t) \sigma_{m1}^{-1} \mathbf{h}_t \mathbf{h}_t^T & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sum_{mt} \gamma_m(t) \sigma_{mD}^{-1} \mathbf{h}_t \mathbf{h}_t^T \end{pmatrix}^{-1}$$

$$\times vec\left(\left(\frac{\partial Q}{\partial \mathbf{U}}\right)^T\right)|_{\mathbf{U} = 0}$$

$$(22)$$

Multiplying the above equation with  $\mathbf{T}_{K,D}^{-1}$  on both sides, we get  $\mathbf{T}_{K,D}^{-1}vec(\mathbf{U})$ 

$$= \begin{pmatrix} \sum_{mt} \gamma_m(t) \sigma_{m1}^{-1} \mathbf{h}_t \mathbf{h}_t^T & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sum_{mt} \gamma_m(t) \sigma_{mD}^{-1} \mathbf{h}_t \mathbf{h}_t^T \end{pmatrix}^{-1} \\ \times vec \left( \left( \frac{\partial Q}{\partial \mathbf{U}} \right)^T \right) |_{\mathbf{U} = 0} \\ = \mathbf{T}_{D,K} vec(\mathbf{U}) \\ = vec(\mathbf{U}^T)$$
 (23)

We therefore have

$$vec(\mathbf{U}^T)$$

$$= \begin{pmatrix} \sum_{mt} \gamma_{m}(t) \sigma_{m1}^{-1} \mathbf{h}_{t} \mathbf{h}_{t}^{T} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sum_{mt} \gamma_{m}(t) \sigma_{mD}^{-1} \mathbf{h}_{t} \mathbf{h}_{t}^{T} \end{pmatrix}^{-1} \times vec \begin{pmatrix} \left(\frac{\partial Q}{\partial \mathbf{U}}\right)^{T}\right) |_{\mathbf{U} = 0} \\ = \begin{pmatrix} \left(\sum_{mt} \gamma_{m}(t) \sigma_{m1}^{-1} \mathbf{h}_{t} \mathbf{h}_{t}^{T}\right)^{-1} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \left(\sum_{mt} \gamma_{m}(t) \sigma_{mD}^{-1} \mathbf{h}_{t} \mathbf{h}_{t}^{T}\right)^{-1} \end{pmatrix} \times vec \begin{pmatrix} \left(\frac{\partial Q}{\partial \mathbf{U}}\right)^{T}\right) |_{\mathbf{U} = 0}$$

$$(24)$$

This indicates that each row of  $\mathbf{U}$ , which is a vector of dimension K, can be updated independently from other rows as in (15).

## A.2. Derivation of an efficient Gauss–Newton algorithm when considering Jacobian term

Using permutation matrix, we rewrite the right hand side of (8) as

$$vec(\mathbf{J}_{t}^{-T})^{T}[\alpha(\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T} \otimes \mathbf{I}_{D\times D}]$$

$$= vec(\mathbf{J}_{t}^{-T})^{T}[\alpha\mathbf{T}_{DD}\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T}]\mathbf{T}_{DK}$$

$$= \alpha(\mathbf{T}_{DD}^{T}vec(\mathbf{J}_{t}^{-T}))^{T}[\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T}]\mathbf{T}_{DK}$$

$$= \alpha vec(\mathbf{J}_{t}^{-1})^{T}[\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T}]\mathbf{T}_{DK}$$

$$= \alpha(\mathbf{T}_{DK}^{T}(vec(\mathbf{J}_{t}^{-1})^{T}\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T})^{T})^{T}$$

$$= \alpha(\mathbf{T}_{KD}(vec(\mathbf{J}_{t}^{-1})^{T}\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T})^{T}$$

$$= \alpha(vec(\mathbf{J}_{t}^{-1})^{T}\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T})^{T}$$

$$= \alpha(vec(\mathbf{J}_{t}^{-1})^{T}\mathbf{I}_{D\times D} \otimes (\mathbf{H}_{t}(\mathbf{I}_{K\times K}-\mathbf{H}_{t})\mathbf{W}_{c})^{T})^{T}$$

$$(25)$$

where  $\mathbf{T}_{DK}$  is a permutation matrix. The above is a vector of dimension  $1 \times DK$ .

#### A.3. Auxiliary scores by fMLLR

fMLLRs can be implemented either as a bias transformation or an affine transformation. In the case of bias transformation, its auxiliary score is

$$Q = -\frac{1}{2} \sum_{mt} (\mathbf{b} - \boldsymbol{\rho}_{mt})^T \boldsymbol{\Sigma}_m^{-1} (\mathbf{b} - \boldsymbol{\rho}_{mt})$$
 (26)

where  $\mathbf{b}$  is a global bias to be added to the input observation  $\mathbf{x}_t$ . In the case of affine transformation, its auxiliary score is as follows:

$$Q = \beta \log(|\mathbf{A}|) - \frac{1}{2} \sum_{d} (\mathbf{w}_{j} \mathbf{G}_{j} \mathbf{w}_{j}^{T} - 2\mathbf{w}_{j} \mathbf{k}_{j}) - \frac{1}{2} \sum_{mt} \gamma_{m}(t) \boldsymbol{\mu}_{m}^{T} \boldsymbol{\Sigma}_{m}^{-1} \boldsymbol{\mu}_{m}$$
 (27)

where  $\mathbf{w}_j$  is the *j*-th row of the transformation [**A**; **b**].  $\mathbf{G}_j$  and  $\mathbf{k}_j$  are the second and first order statistics for fMLLR estimations [10].

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He has been granted over 60 US or international patents in acoustics/audio, speech/language technology, machine learning (deep learning), and related fields. He received numerous awards/honors bestowed by IEEE, ISCA, ASA, Microsoft, and other organizations. He is a Fellow of the Acoustical Society of America, a Fellow of the IEEE, and a Fellow of ISCA. He served on the Board of Governors of the IEEE Signal Processing Society (2008–2010). More recently, he served as Editor-in-Chief for the IEEE Signal Processing Magazine (2009–2011), which, according to the Thomson Reuters Journal Citation Report released on June 2010 and 2011, ranks first in both years among all IEEE publications (127 in total) and all publications within the Electrical and Electronics Engineering Category worldwide (247 in total) in terms of its impact factor: 4.9 and 6.0, and for which he received the 2011 IEEE SPS Meritorious Service Award. He currently serves as an Editor-in-Chief for the IEEE Transactions on Audio, Speech, and Langauge Processing 2012–2014.

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